

Dados los puntos:

(0.1,-1), (0.8,0.95), (1.2,1.8), (1.2,1.9), (1.7,2.1) y (2.5,3.6)

Encontrar la recta que aproxima la nube de puntos por mínimos cuadrados

S_j	S_j^2	Y_j	$S_j Y_j$
0.1	0.01	-1	-0.1
0.8	0.64	0.95	0.76
1.2	1.44	1.8	2.16
1.2	1.44	1.9	2.28
1.7	2.89	2.1	3.57
2.5	6.25	3.6	9
$\Sigma = 7.5$	$\Sigma = 12.67$	$\Sigma = 9.35$	$\Sigma = 17.67$

$$\begin{cases} 6 \cdot a + b \sum_{j=1}^6 s_j = \sum_{j=1}^6 y_j \\ a \sum_{j=1}^6 s_j + b \sum_{j=1}^6 s_j^2 = \sum_{j=1}^6 (s_j y_j) \end{cases} \longrightarrow \begin{cases} 6a + 7.5b = 9.35 \quad * \\ a(7.5) + 12.67b = 17.67 \end{cases}$$

Se despeja el sistema de ecuaciones: en este caso por sustitución

$$a = \left(\frac{9.35 - 7.5b}{6} \right)$$

$$* 7.5 \left(\frac{9.35 - 7.5b}{6} \right) + 12.67b = 17.67$$

$$\frac{70.125 - 56.25b}{6} + \frac{76.02b}{6} = \frac{106.02}{6}$$

$$7 \cdot 70.125 + 19.77b = 106.02$$

$$13.77b = 106.02 - 70.125$$

$$b = 35.895 / 19.77 = \underline{1.815629742}$$

$$a = \left(\frac{9.35 - 7.5(1.815629742)}{6} \right) = \underline{-0.7112038442}$$

Usando que $r(x) = a + bx$, concluimos que $r(x) = -0.7112038442 + 1.815629742x$